

## Chapter 3

# Bayesian Model Selection (BMS)

### 3.1 BMS.mat file

The BMS structure saved in BMS.mat file contains the following variables<sup>1</sup>:

**BMS.DCM.ffx/rfx** (fixed-effects (FFX) / random-effects (RFX) analysis)

<b>.data</b>	path to model_space.mat file (see below).
<b>.F_fname</b>	path to file containing the log evidence matrix, F, (if this option is specified).
<b>.F</b>	matrix of log model evidences for all subjects and models, [nsub × nm].
<b>.SF</b>	vector of summed log evidences over subjects [1 × nm].
<b>.model</b>	results from model level inference (see below).
<b>.family</b>	results from family level inference (see below).
<b>.bma</b>	results from Bayesian model averaging (see below).

#### 3.1.1 Model level results

Fixed-effects:

<b>model</b>	
<b>.prior</b>	model priors, $p(m)$ , [1 × nm].
<b>.subj_lme</b>	log model evidence matrix, [nsub × nm].
<b>.like</b>	model likelihoods, $p(Y m)$ , [1 × nm].
<b>.posts</b>	model posterior probabilities, $p(m Y)$ , [1 × nm].

Random-effects (different from fixed-effects):

<b>model</b>	
<b>.alpha0</b>	initial Dirichlet parameters (prior counts), $\alpha_0$ , [1 × nm].
<b>.exp_r</b>	model posterior means, $\langle r Y \rangle$ , [1 × nm].
<b>.xp</b>	model exceedance probabilities, $\psi_m$ [1 × nm].
<b>.r_samp</b>	samples from the model posterior density, $p(r Y)$ , [nsamp × nm].
<b>.g_post</b>	posterior model probabilities for subject n and model m, $p(m_n Y)$ , [nsub × nm].

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<sup>1</sup>nm = number of models; nfm = number of families; nsub = number of subjects; nsamp = number of samples; dima/b/c/d = dimensions of a/b/c/d DCM parameters; np = number of model parameters; nsess = number of sessions.

### 3.1.2 Family level results

Fixed-effects:

<b>family</b>	
<b>.names</b>	family names, ex: {'F1', 'F2', 'F3'}.
<b>.partition</b>	partition vector assigning each model to a family [ $1 \times nm$ ].
<b>.infer</b>	inference method ('ffx' or 'rfx').
<b>.prior</b>	family priors, $p(f_k)$ , [ $1 \times nfam$ ].
<b>.post</b>	family posterior probabilities, $p(f_k Y)$ , [ $1 \times nfam$ ].
<b>.like</b>	family likelihoods, $p(Y f_k)$ , [ $1 \times nfam$ ].

Random-effects (different from fixed-effects):

<b>family</b>	
<b>.Nsamp</b>	number of samples used in Gibbs sampling (default = 20000).
<b>.prior</b>	family type of priors ('F-unity', $\alpha_0 = 1$ , for each family, is the default; other option, 'M-unity', $\alpha_0 = 1$ , for each model) .
<b>.alpha0</b>	initial values of the Dirichlet parameters (prior counts), $\alpha_{prior}(m)$ , [ $1 \times nfam$ ].
<b>.s_samp</b>	samples from family posterior density, $p(s Y)$ , [ $nsamp \times nfam$ ].
<b>.exp_r</b>	family posterior means, $\langle s_k Y \rangle$ , [ $1 \times nfam$ ].
<b>.xp</b>	family exceedance probabilities, $\psi_k$ , [ $1 \times nfam$ ].

### 3.1.3 Bayesian model averaging (BMA)

Fixed-effects:

<b>bma</b>	
<b>.nsamp</b>	number of samples used to average parameters (default = 10000).
<b>.odds_ratio</b>	posterior odds ratio, $\pi_{OCC}$ , (number of models in Occams window, default = 0).
<b>.Nocc</b>	number of models in Occam's window.
<b>.Mocc</b>	index of models in Occam's window, [ $1 \times nm$ ].
<b>.indx</b>	index of models in Occam's window (different for each subject in RFX), [ $1 \times nm$ ].
<b>.theta</b>	samples from the parameter posterior density, $p(\theta Y)$ , [ $np \times nsamp$ ];
<b>.theta_sbj</b>	samples from the parameter posterior density, $p(\theta Y)$ , for each subject, [ $np \times nsub \times nsamp$ ];
<b>.mtheta_sbj</b>	mean parameters for each subject, [ $np \times nsub$ ];
<b>.stheta_sbj</b>	standard deviation of the parameters for each subject [ $np \times nsub$ ];
<b>.a</b>	samples from posterior density over DCM.a parameters [ $dima \times nsamp$ ].
<b>.b</b>	samples from posterior density over DCM.b parameters [ $dimb \times nsamp$ ].
<b>.c</b>	samples from posterior density over DCM.c parameters [ $dimc \times nsamp$ ].
<b>.d</b>	samples from posterior density over DCM.d parameters [ $dimd \times nsamp$ ].
<b>.post</b>	model posterior probabilities for each subject, $p(m Y)$ , [ $nsub \times nm$ ].
<b>.ma</b>	mean DCM.a parameters, [ $dima$ ].
<b>.mb</b>	mean DCM.b parameters, [ $dimb$ ].
<b>.mc</b>	mean DCM.c parameters, [ $dimc$ ].
<b>.md</b>	mean DCM.d parameters, [ $dimd$ ].

Random-effects - same variables as in fixed-effects.

## 3.2 model\_space.mat file

This structure is created automatically if it doesn't exist in the chosen directory and can be loaded for subsequent analyses as a faster option to reading the DCM.mat files. The model\_space.mat

file contains the following structure:

<b>subj(nsub).sess(nsess).model(nm)</b>	
<b>.fname</b>	path to DCM.mat file.
<b>.F</b>	log-evidence (free energy).
<b>.Ep</b>	parameter estimates: conditional expectation, [np × 1].
<b>.Cp</b>	parameter estimates: conditional covariance, [np × np].

For a detailed description of all the variables and methods please see [\[56\]](#) and [\[60\]](#).