## envstat list

Home page - meeting info etc.
http://www.jiscmail.ac.uk/files/envstat
Message archives
http://www.jiscmail.ac.uk/lists/envstat.html
E-mail subscription
envstat-subscribe-request@jiscmail.ac.uk
envstat-signoff-request@jiscmail.ac.uk
Contact list owner
envstat-request@jiscmail.ac.uk
Send messages
envstat@jiscmail.ac.uk

## Trends in temperatures: exploration and estimation

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## Outline

1. Central England Temperature

- Long series - data meeting
- Monthly patterns
- Aggregation
- Shorter series

2. CET daily

- Annual extremes
- Other functionals (timing)
- Monthly extremes
- Shorter series


## 1. Central England Temperature

- Average of several sites in "Central England"
- Bristol, Manchester, London
- data meeting
- Average monthly temperature
- 341 years
- 4092 observations





### 1.1 Annual - linear trend

|  | Rise 'C/100Y | $\mathbf{p}$ | rho1 |
| :--- | ---: | ---: | ---: |
| Annual Mean | 0.226 | 0.000 | $\mathbf{0 . 2 2}$ |
| With AR(1) | 0.227 | 0.000 |  |
| $1878-$ | 0.773 | 0.000 | $\mathbf{0 . 1 7}$ |

- rhol>0.11, reduces significance



### 1.2 Seasons - linear trend

| Season | Rise ${ }^{‘} \mathbf{C}$ <br> $/ \mathbf{1 0 0 Y}$ | $\mathbf{p}$ | rho1 |
| :--- | ---: | ---: | ---: |
| DJF | 0.35 | 0.000 | -0.01 |
| MAM | 0.23 | 0.000 | $\mathbf{0 . 1 9}$ |
| JJA | 0.06 | 0.179 | 0.10 |
| SON | 0.25 | 0.000 | $\mathbf{0 . 2 0}$ |



### 1.3 Seasons - shorter series

| Season | $\mathbf{a l l}$ | $\mathbf{1 8 7 8}$ | $\mathbf{p}$ | rho1 |
| :--- | ---: | ---: | ---: | ---: |
| DJF | 0.35 | $\mathbf{0 . 5 5}$ | 0.101 | 0.10 |
| MAM | 0.23 | $\mathbf{0 . 7 4}$ | 0.000 | 0.13 |
| JJA | 0.06 | $\mathbf{0 . 6 4}$ | 0.003 | -0.01 |
| SON | 0.25 | $\mathbf{1 . 0 9}$ | 0.000 | 0.00 |

### 1.4 Months

- Smooth variation through year
- Are trends better-defined by not aggregating?


| Month | Trend 'C/100Y | $\mathbf{p}$ | rho1 |
| :--- | ---: | ---: | ---: |
| December | 0.36 | 0.000 | 0.02 |
| January | 0.44 | 0.000 | 0.01 |
| February | 0.27 | 0.008 | -0.05 |
| March | 0.38 | 0.000 | 0.07 |
| April | 0.20 | 0.002 | 0.12 |
| May | 0.11 | 0.072 | 0.15 |
| June | -0.02 | 0.736 | -0.06 |
| July | 0.11 | 0.086 | 0.04 |
| August | 0.11 | 0.070 | 0.15 |
| September | 0.15 | 0.010 | 0.15 |
| October | 0.32 | 0.000 | 0.09 |
| November | 0.30 | 0.000 | 0.07 |



## 1.4a Monthly vs annual?

- Trade-off is variance: annual confidence intervals are $1 / \mathrm{sqrt}(12)=0.29$ of monthly
- But averaging obviously different trends brings estimate towards zero
- Should model structure


### 1.5 Months - shorter series

- 1878- only
- Trade-off - shorter length reduces precision, but trends may be larger
- Can also consider short series at various points
- sensitivity of 100 Y trend




### 1.6 One model? Heterogeneity

- Could put all months together
- if variances are homogeneous
- Slight summer/winter heterogeneity
- One model saves 11 variance d-o-f
- For large samples, relatively little benefit



### 1.7 Changing seasons

- Different trends in different months - changing seasonal pattern
- Seasonal cycle has become (slightly) compressed




### 1.8 Linear modelling assumptions?

- Normal
- symmetry for estimation
- full Normality for significance
- data are averages
- Independence
- autocorrelation - okay for season/month lags




## 2. Daily series

- 1772-
- Can now look at other characteristics
- 227 annual extremes (each of 365+ values)
- As well as actual value, consider timing:
- min is usually in January
- and max is usually in July
- Other functionals - degree days



### 2.1 Trends in (annual) extremes

- Summer maxima
- no trend ( $\mathrm{p}=0.13$ )
- Winter (overlapping Dec) minima

|  | Trend 'C/C | s.e. |
| :--- | ---: | ---: |
| Linear | 0.87 | 0.24 |
| GEV | 0.67 | 0.22 |

### 2.2 Monthly extremes

- 30 (ish) values
- 30 daily temperatures - extremes
- Monthly minima
- Monthly maxima



### 2.3 Shorter data series

- As before, consider 1878-
- Trends/changes somewhat stronger





## 3. Remarks

- Linear trends are useful exploratory tools
- Take account of:
- structure - seasons
- heterogeneity - may not put everything in one model
- autocorrelation? May be small effect at seasonal lag
- data length - trade-off strength and consistency vs significance
- other forms of pooling (sites)
- Look at patterns/trends in functionals of interest (timing, cumulative)

